

Progressive Education Society's Modern College of Arts, Science & Commerce, Ganeshkhind , Pune – 16

End Semester Examination: Jan.2023 Faculty: Science and Technology

Program: B.ScComp05 Semester: I SET: C

Program (Specific): B.Sc.Comp. Science Course Type: Core

Class: F.Y. B. Sc (Comp. Sci.)

Max. Marks: 35 Name of the Course: Discrete Mathematics

Course Code:22-MTC-112 Time: 2Hr

Paper: II

Instructions to the candidate:

- 1) There are 4 sections in the question paper. Write each section on separate page.
- 2) All Sections are compulsory.
- 3) Figures to the right indicate full marks.
- 4) Draw a well labelled diagram wherever necessary.

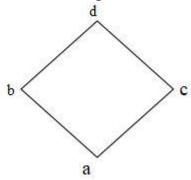
SECTION: A

Q1) Choose the correct option.

(5 Marks)

- i) The inverse of the statement $p \rightarrow q$ is
 - a) $q \rightarrow p$
 - b) $\neg p \rightarrow \neg q$
 - c) $\neg q \rightarrow \neg p$
 - d) $p \rightarrow \neg q$
- ii) Let P(x): x < 3 then the truth values of P(-1) and P(6) respectively are
 - a) T, F
 - b) F,T

- c) T, T
- d) F, F
- iii) In the poset $(D_{10}, |)$ the g.l.b. of (2, 5) is
 - a) 2
 - b) 5
 - c) 1
 - d) 10
- iv) The Hasse diagram is the representation of which of the following Lattices



- a) D_4
- b) *D*₁₂
- c) D₅
- d) D_6
- v) There are 8 men and 7 women. In how many ways a committee of 4 men and 3 women can be formed?
- a) $8_{C_3} + 7_{C_4}$
- b) $8_{\mathcal{C}_3} . 7_{\mathcal{C}_4}$
- c) $8_{\mathcal{C}_4}$. $7_{\mathcal{C}_3}$
- d) $8_{C_4} + 7_{C_3}$

Q2) Attempt any 4 out of 6.

(4 Marks)

- i) Define an antisymmetric relation.
- ii) Write the negation of the following statement.

$$\forall x (x^2 > x).$$

- iii) Draw the Hasse diagram of $D_{18} = \{1,2,3,6,9,18\}$ with the relation R defined as xRy iff x divides y, \forall x, y \in D_{18}
- iv) Find the characteristic equation corresponding to the recurrence relation

$$a_r + 6a_{r-1} + 9a_{r-2} = 0$$

- v) How many 4 letter words can be formed using a,e,i,o and u without repetition?
- vi) If A and B are two subsets of a finite set U with |A| = 30, |B| = 40 and $|A \cap B| = 20$, then find $|A \cup B|$.

SECTION: B

Q3) Attempt any 4 out 6

(8 Marks)

- i) Check whether the propositions $\neg q \rightarrow \neg p$ and $(p \rightarrow q)$ are logically equivalent.
- ii) Use logical connectives and propositions p and q given below, to convert the following statements into symbolic form .

p: It is below freezing..

q: It is snowing.

- a) It is below freezing and snowing.
- b) If it is below freezing then it is snowing.
- iii) Identify the relation set R and draw the digraph from the matrix of relation R given below

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$$M(R) \ = \ \left(\begin{array}{cccc} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{array} \right) \text{ on the set A = \{1,2,3,4\}}.$$

- iv) Show that the set $S = \{1,3,5,15\}$ with the relation R is a lattice, where R is defined as xRy iff x divides y.
- v) How many positive integers less than 1000 are divisible by 2 and 7?
- vi) Solve the recurrence relation

$$a_r - 6a_{r-1} + 9a_{r-2} = 0$$

SECTION: C

Q4) Attempt any 4 out of 6.

(8 Marks)

- i) Translate the following statement into logical expression using predicates, quantifiers and connectives, where the universe of Discourse is the set of integers.
 - "For each value of x, there is a value of y such that x + y = 12".
- ii) Using pigeon hole principle show that if 5 integers are selected from the first 8 positive integers, then there must be a pair of these integers with sum equal to 9.
- iii) Discuss whether the following relation defined on the set A= {a, b, c} is reflexive and symmetric, where R = { (a, a), (b, b), (c, c), (a, b) }.
- iv) Define a distributive lattice and give an example.
- v) How many name plates can be made using 3 letters followed by 3 digits?
- vi) Given 7 different Hindi books, 9 different Marathi books and 5 different English books, how many ways are there to select one book of each language?

SECTION: D

Q5) Attempt any 2 out of 4.

(10 Marks)

- i) Find the Disjunctive Normal Form of the Boolean function $f(x, y, z) = (x \land \overline{(y \lor z)}) \lor (z \land y)$.
- ii) Test the validity of the following argument by direct method.

$$\neg p \land q, r \rightarrow p, \neg r \rightarrow s, s \rightarrow t \mid t$$

- iii) Find the particular solution of the recurrence relation $a_r 5a_{r-1} = 2^r$, with $a_1 = 20$.
- iv) Using Warshall's algorithm, obtain transitive closure of the relation $R = \{(1, 1), (1, 2), (2, 3), (3, 1), (3, 2)\}$ defined on the set $A = \{1, 2, 3\}$.